

Heavy Ions Collisions and the search for the Quark-Gluon Plasma

Carlos A. Salgado

CERN, TH-Division

(carlos.salgado@cern.ch, <http://home.cern.ch/csalgado>)

1. QCD matter. The final state in HIC.
2. The first stages and before. The initial state in HIC.
3. Signals for the QGP formation.
4. Experimental/Theoretical status.
 - ⇒ RHIC
 - ⇒ LHC

Summary I+II

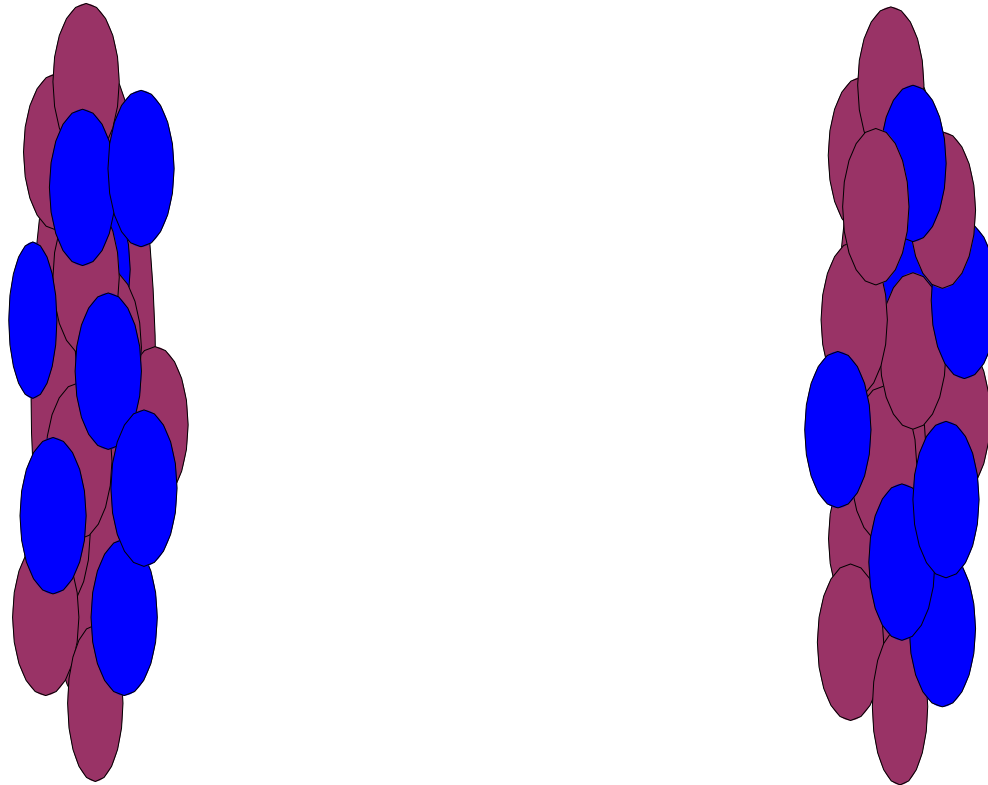
- ⇒ QCD vacuum:
Confinement & chiral symmetry breaking
- ⇒ Theory → Different phases exist!
- ⇒ Order of the transition depends on quarks masses. For realistic masses, most probably crossover at $\mu_B = 0$.
Initial state effects
- ⇒ Multiple scattering and coherence effects necessary to describe heavy ion collisions
- ⇒ Large multiplicities in HIC
 - ↪ High densities created
- ⇒ Non-linear terms in the evolution equations appear.

3. Signals of QGP formation

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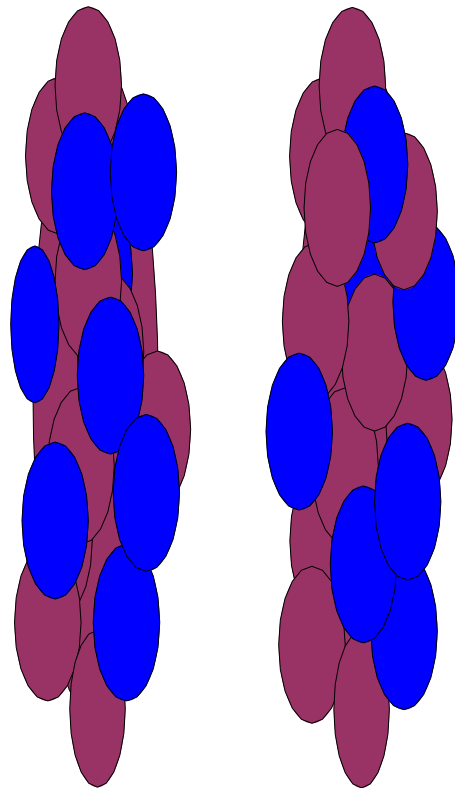
Final state effects

High-energy heavy ion collisions



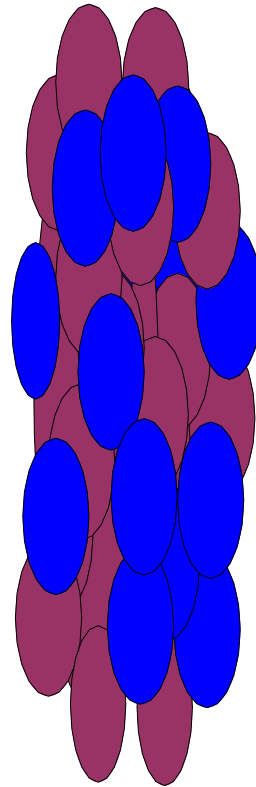
Before the collision: Lorentz-contracted nuclei

High-energy heavy ion collisions



Before the collision: Lorentz-contracted nuclei

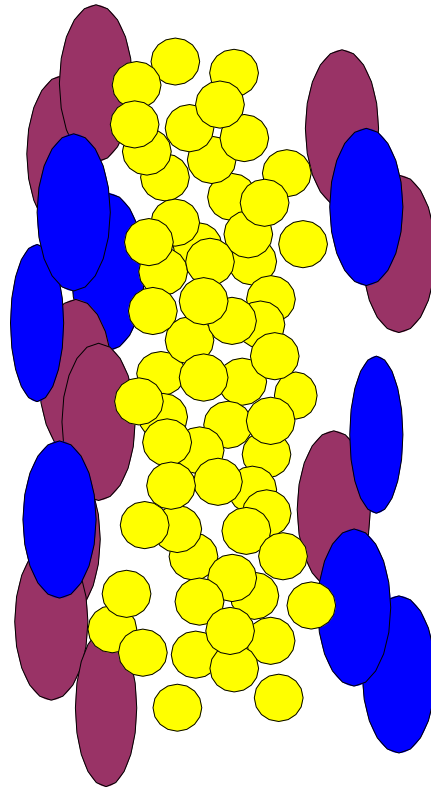
High-energy heavy ion collisions



at $t = 0$ most of the energy in the central region

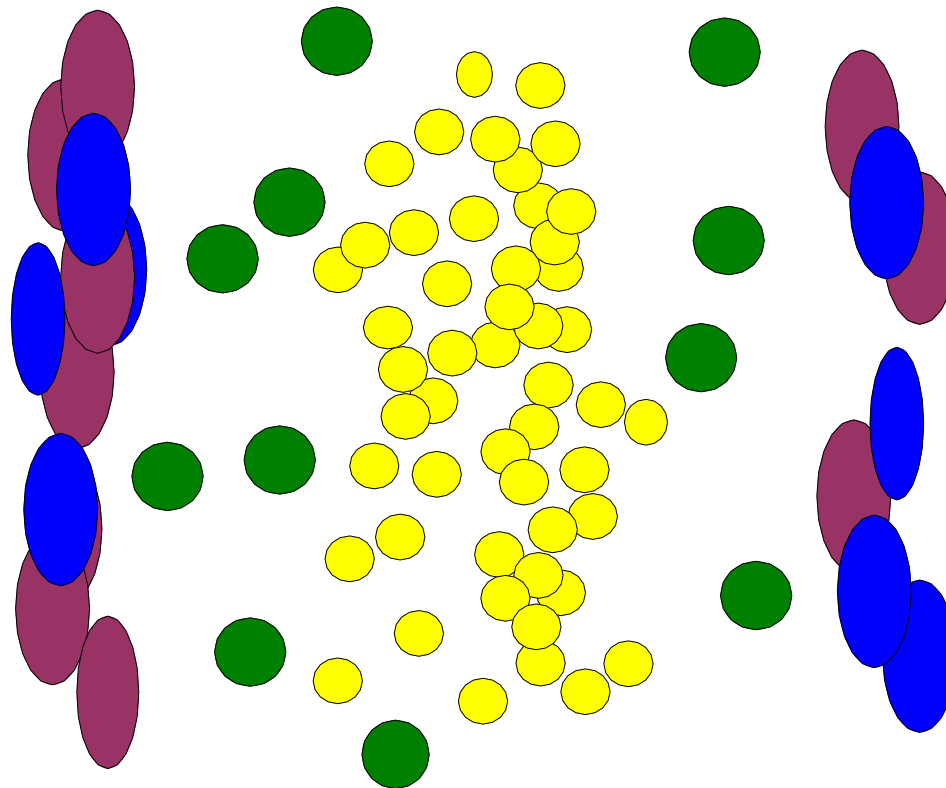
Initial state

High-energy heavy ion collisions



First $\sim 0.1 \div 0.3$ fm. Quark gluon plasma formation

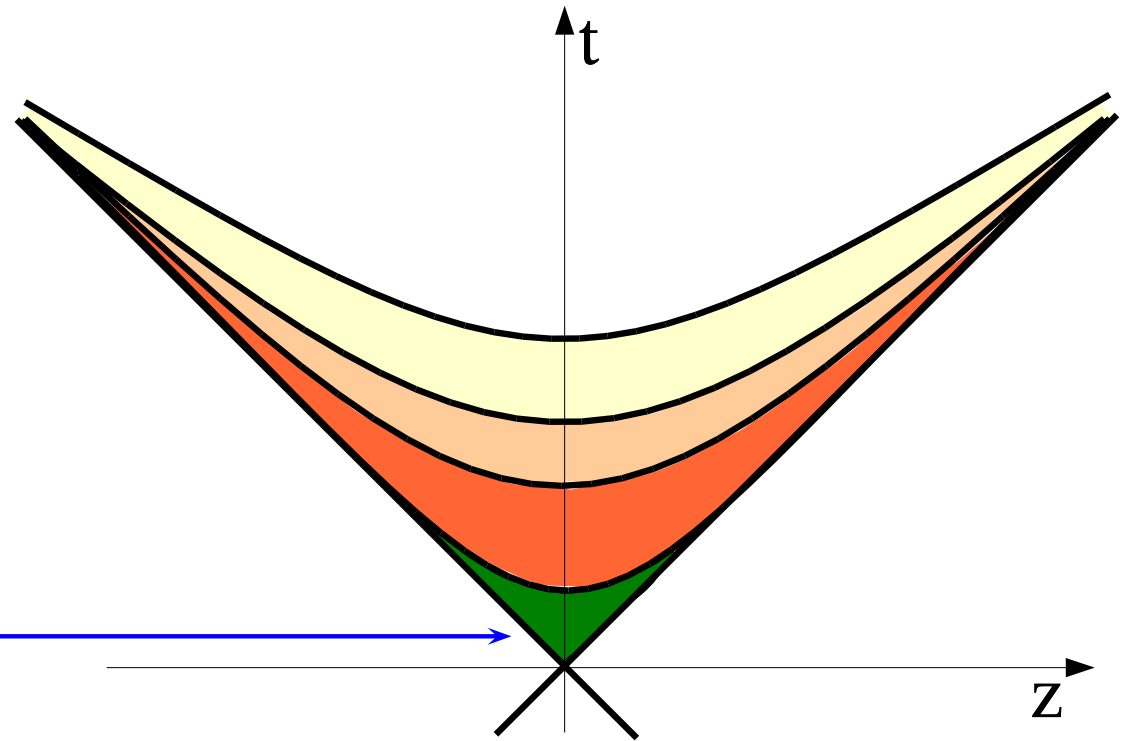
High-energy heavy ion collisions



Expansion and hadronization

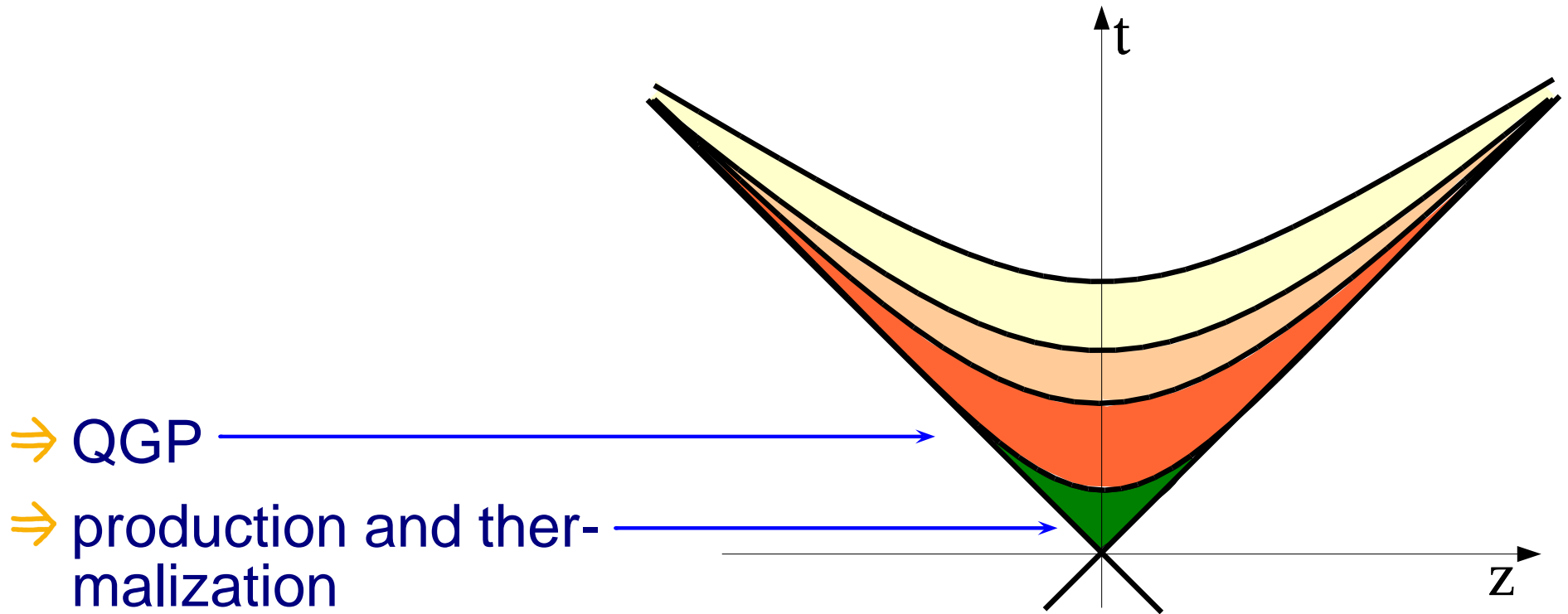
"Canonical" space-time picture

⇒ production and thermalization



Transitions: lines of constant proper time τ .

"Canonical" space-time picture



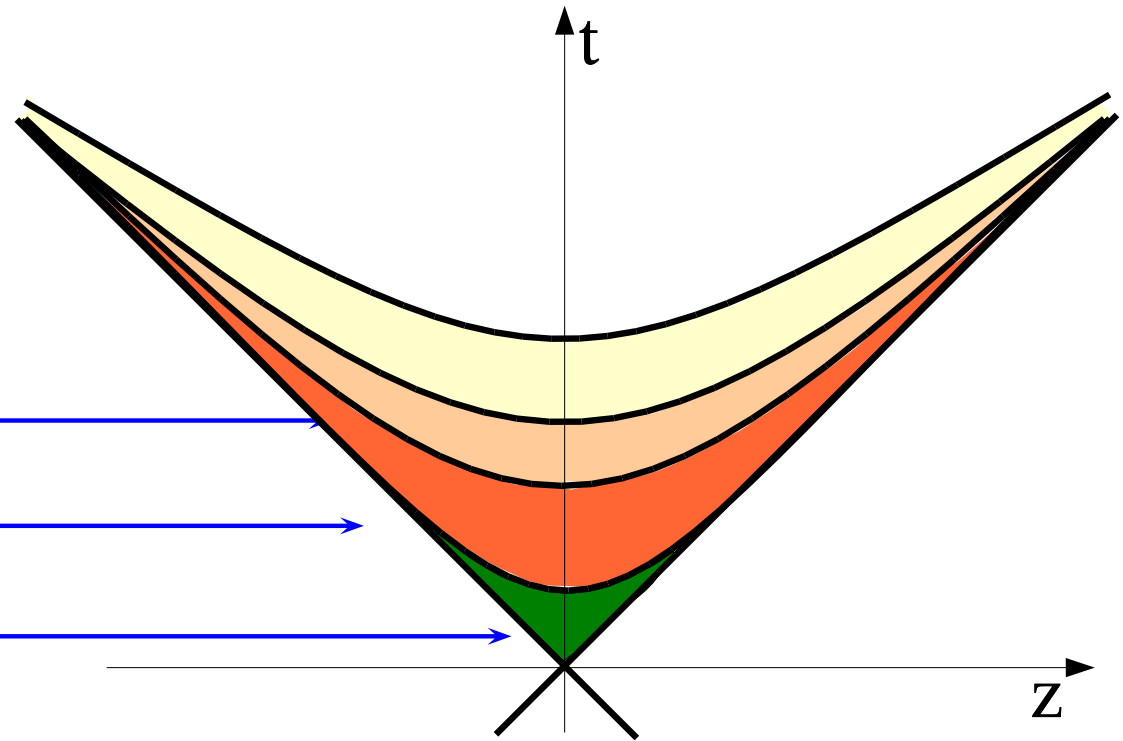
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⇒ mixed phase??

⇒ QGP

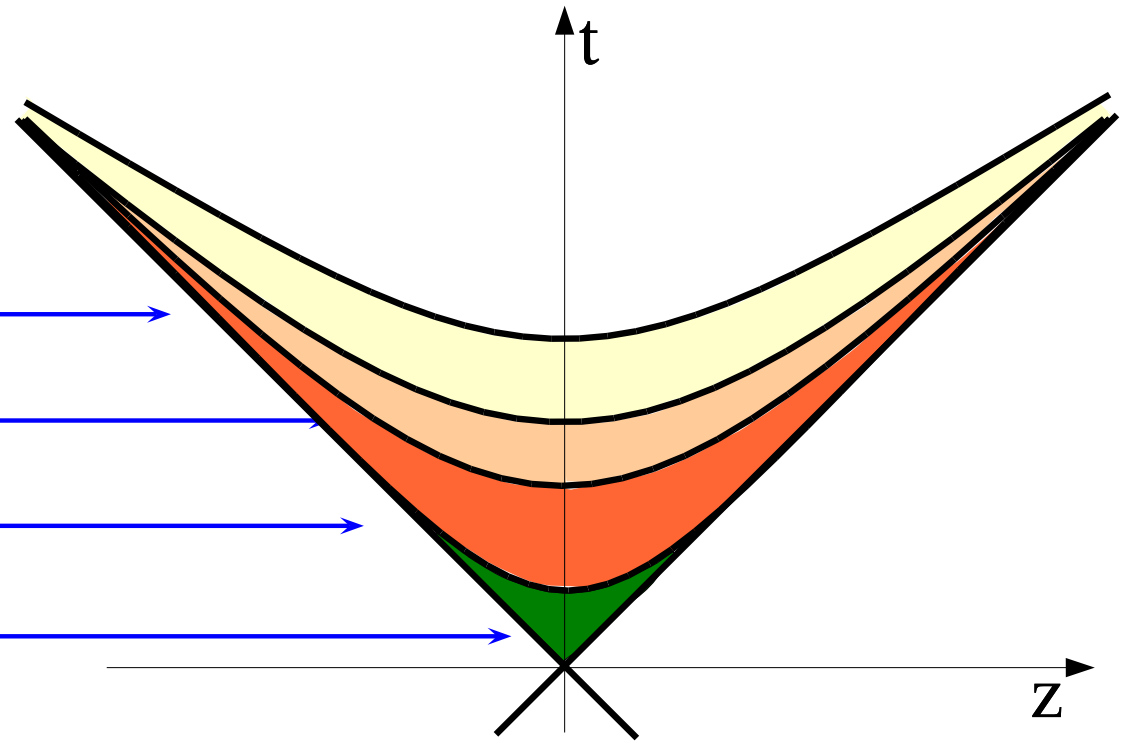
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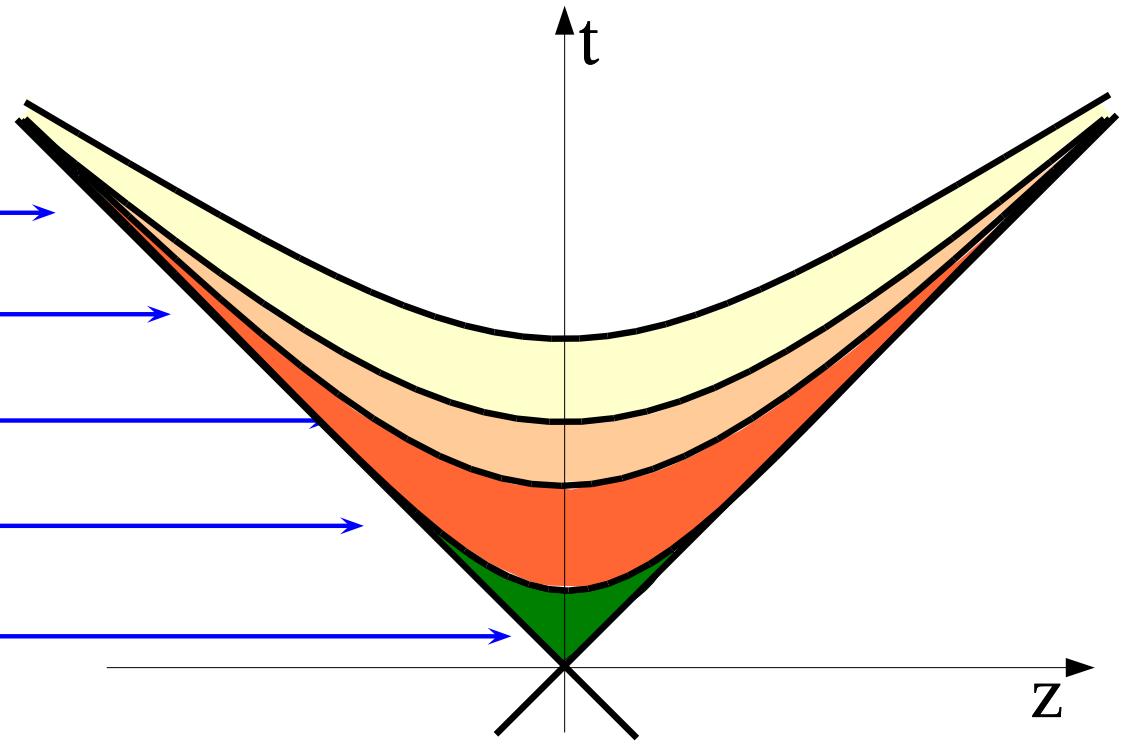
- ⇒ hadron gas
- ⇒ mixed phase??
- ⇒ QGP
- ⇒ production and thermalization



Transitions: lines of constant proper time τ .

"Canonical" space-time picture

- ⇒ freeze-out
- ⇒ hadron gas
- ⇒ mixed phase??
- ⇒ QGP
- ⇒ production and thermalization



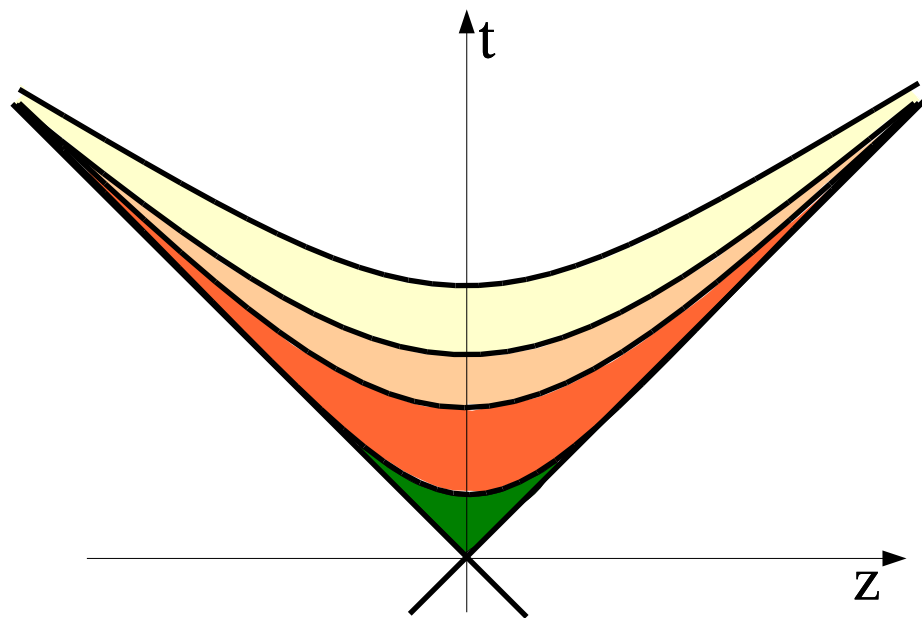
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Characterization of the medium

The medium (or media?!), if formed, has a very short lifetime. In order to study its properties some (indirect) signals are proposed

⇒ Soft (bulk) signatures:

- ↘ Strangeness enhancement
- ↘ Flows
- ↘ Particle composition
- ↘ ...



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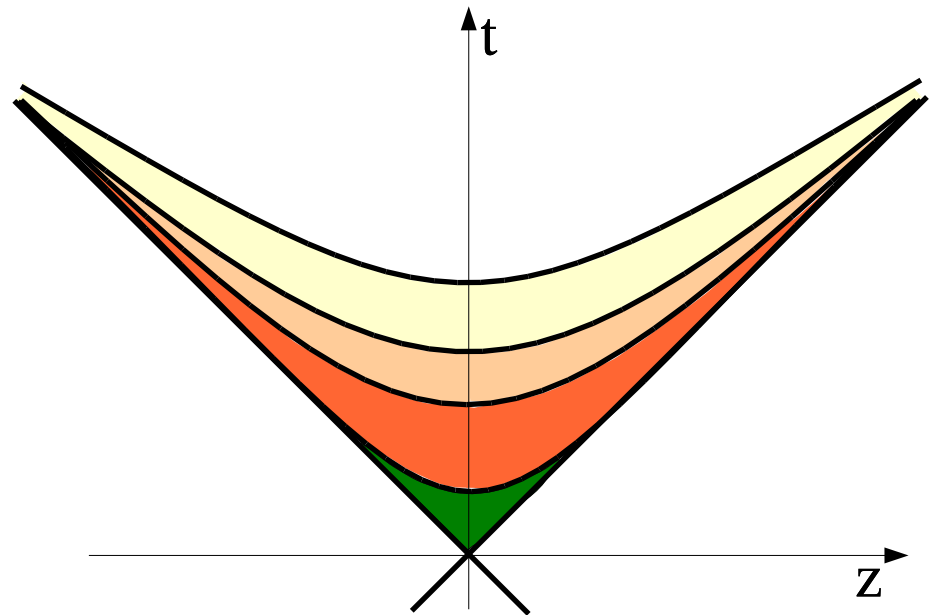
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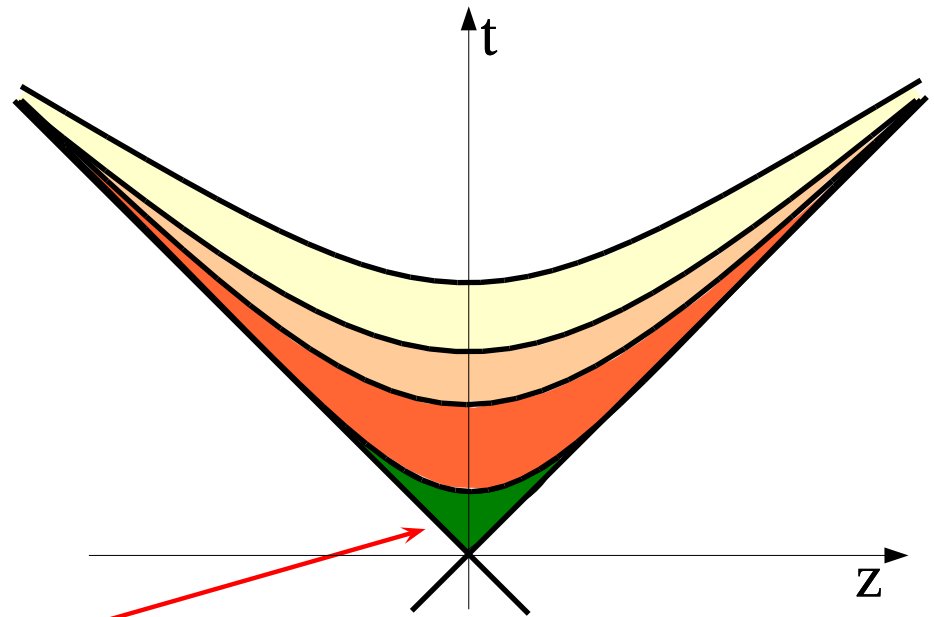
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Produced at the early ($\tau \sim 1/Q$) stages



Soft probes

Strangeness enhancement

In order to produce strangeness, in a medium with broken chiral symmetry one needs

$$m_{K^+} + m_{K^-} \sim 1\text{GeV}$$

In a medium in which chiral symmetry is restored, the energy is just the sum of the strange quark mass,

$$m_s + m_{\bar{s}} \sim 150 \div 400\text{MeV}$$

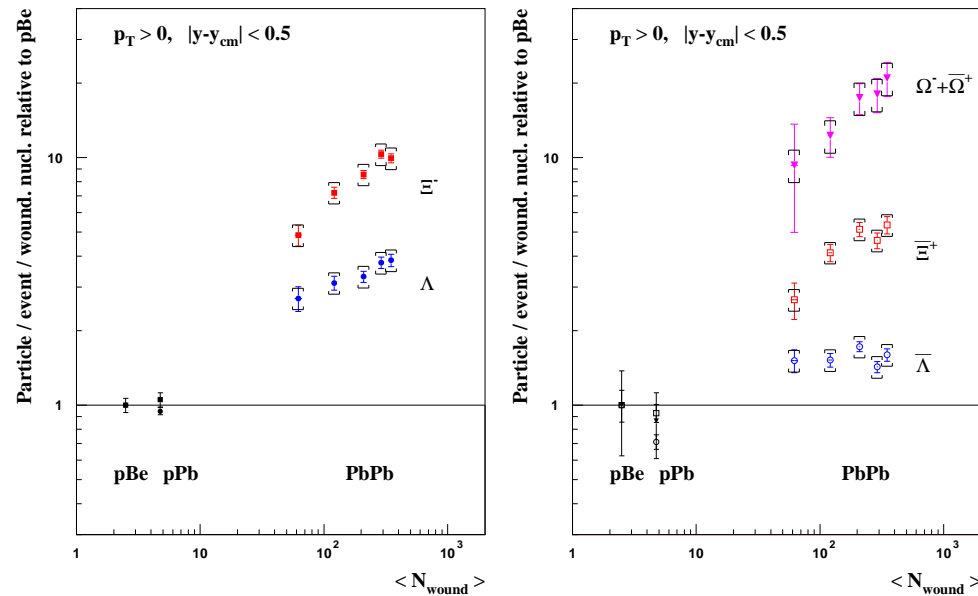
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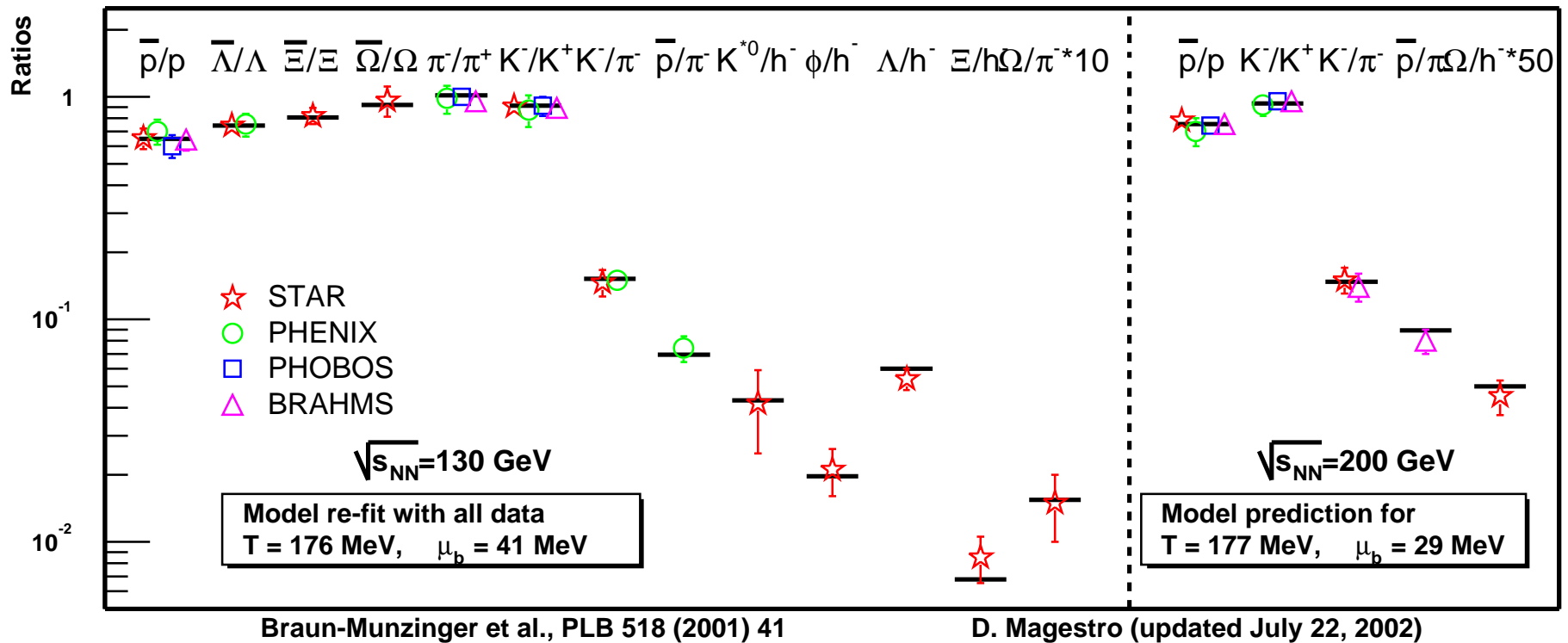
Strange baryons enhancement by NA57 ($\sqrt{s}=17.3\text{ GeV}$)

Statistical description of particle yields

Assuming an ideal gas of particles, the number densities are

$$n_i = -\frac{T}{V} \frac{\partial \ln Z}{\partial \mu_i} \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

Only two independent parameters, μ_B and T (+some assumptions)

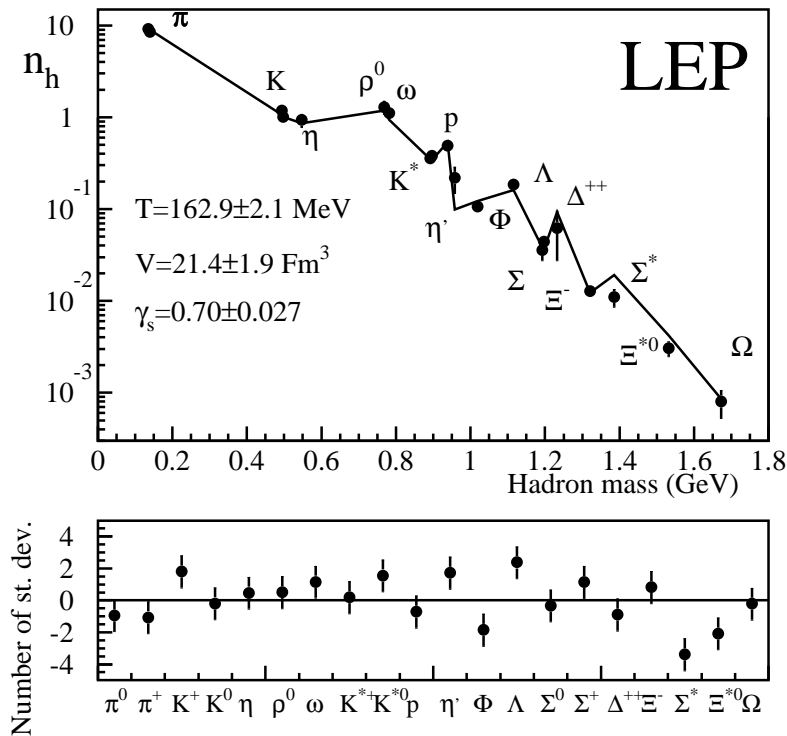


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However, it also works for e^+e^- ...



[Becattini 1995]

Collective flow

⇒ In a non-relativistic fluid, the fluid acceleration is given by Euler's eq.

$$\frac{d\beta}{dt} = -\frac{1}{\rho} \nabla P \quad \left[\frac{d\beta}{dt} = -\frac{c^2}{\epsilon + P} \nabla P \rightarrow \text{relativistic} \right]$$

where, β is the fluid velocity, ρ the mass density and P the pressure.
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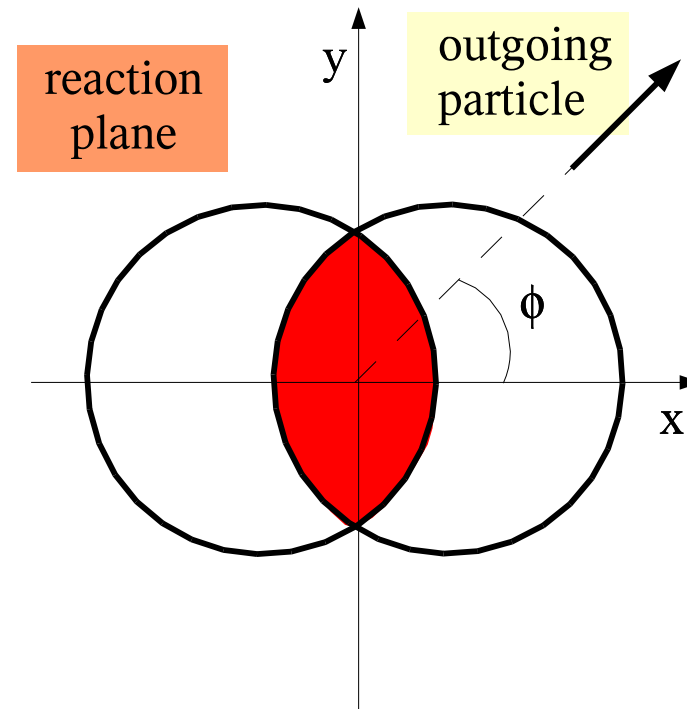
⇒ Initial condition in a HIC has gradients of energy density. This translates into gradients of the pressure and, by evolution, flow.

- ↪ Relation between the initial distribution of energy and flow(s).

Elliptic flow

Gradients are more easily produced in asymmetric media: Changing the centrality of the collision.

⇒ Reaction plane defined by the impact parameter and the collision axis.



Elliptic flow

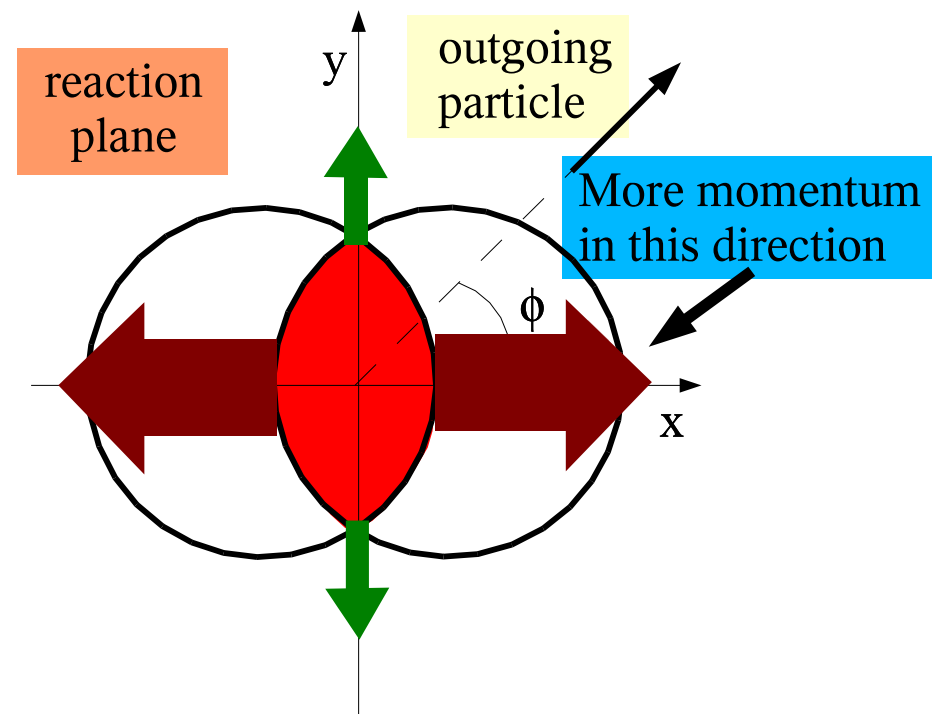
Gradients are more easily produced in asymmetric media: Changing the centrality of the collision.

- ⇒ Reaction plane defined by the impact parameter and the collision axis.
- ⇒ Doing the Fourier expansion of the number of particles in the reaction plane

$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n \cos(n\phi)$$

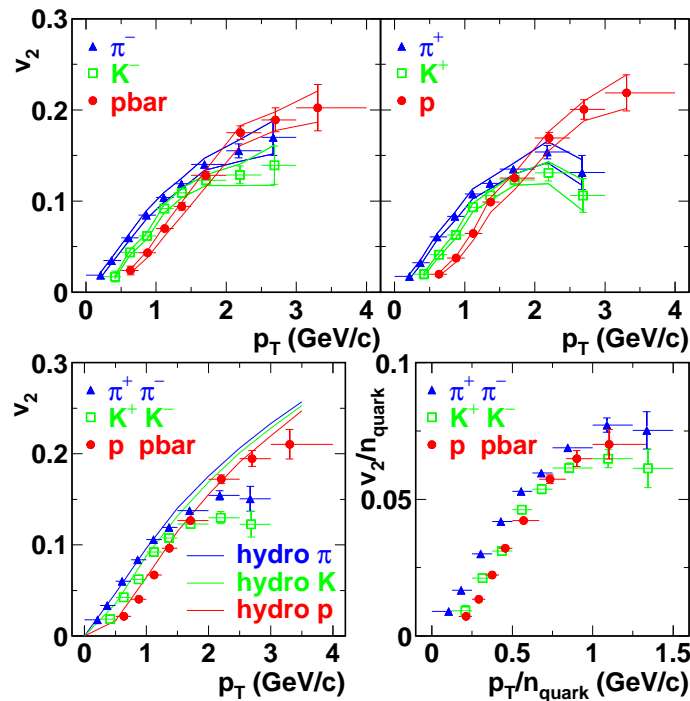
v_n characterize the strength of the anisotropic flow.

- ⇒ v_2 elliptic flow.



Elliptic flow

Elliptic flow has measured at RHIC (one of the main signals)



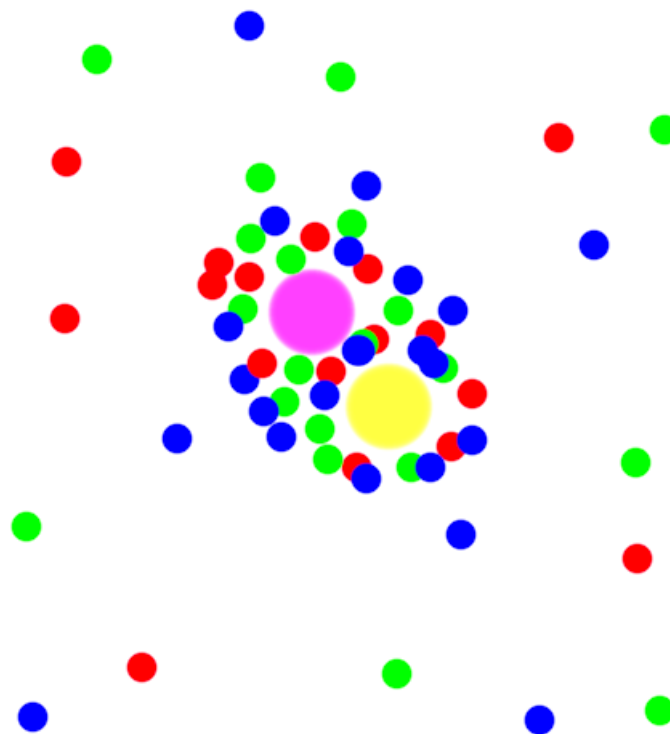
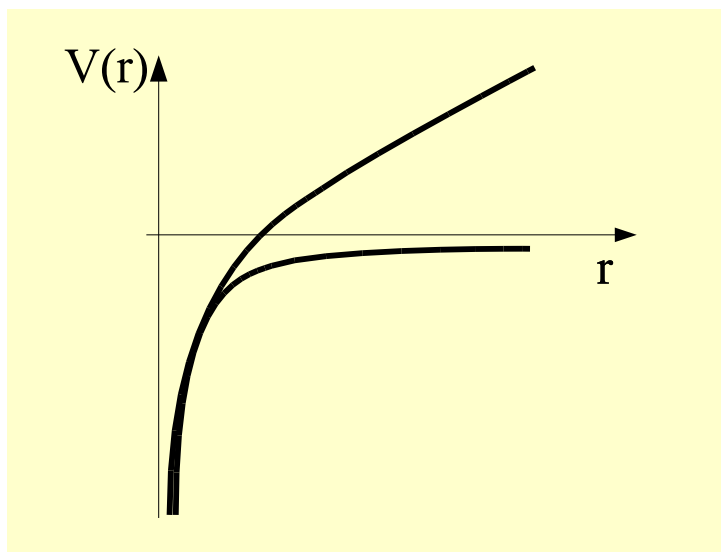
[STAR data]

- ⇒ Comparison with hydrodynamical calculations
- ⇒ The main interest of elliptic flow is that it is very difficult to generate without strong final state interactions/thermalization.

Hard Probes

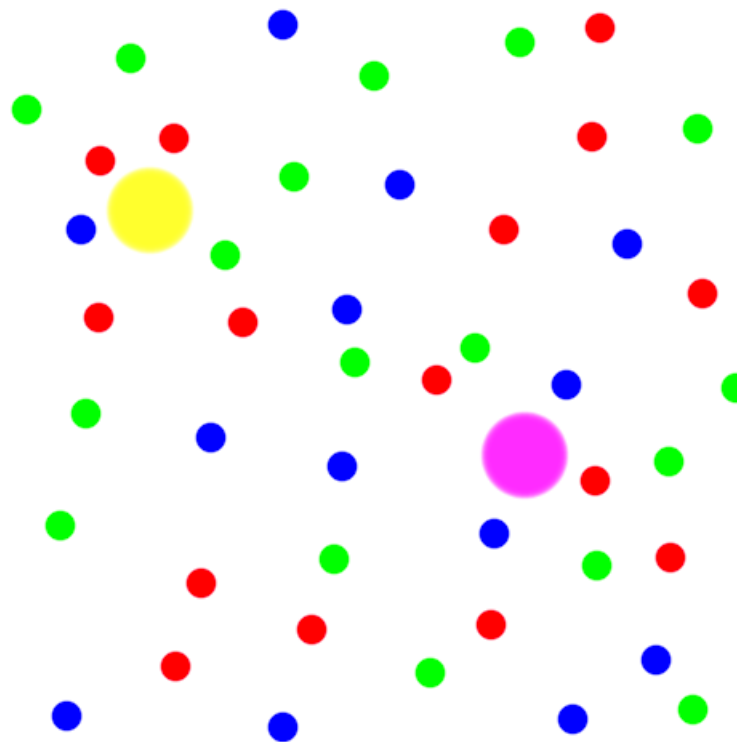
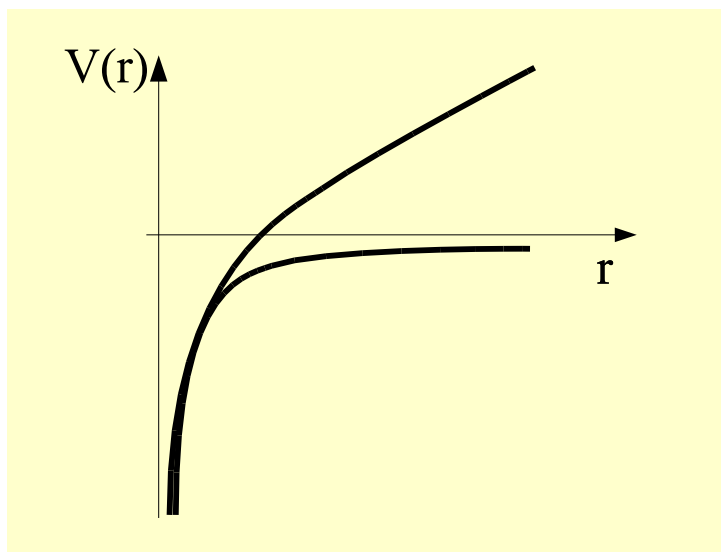
J/Ψ suppression

- ⇒ A J/Ψ is a bound $c\bar{c}$ state.
- ⇒ We have seen that the potential between two quarks is screened in the medium.
- ⇒ In this case, the $c\bar{c}$ pair is diluted in the medium and the production of bound states is suppressed.

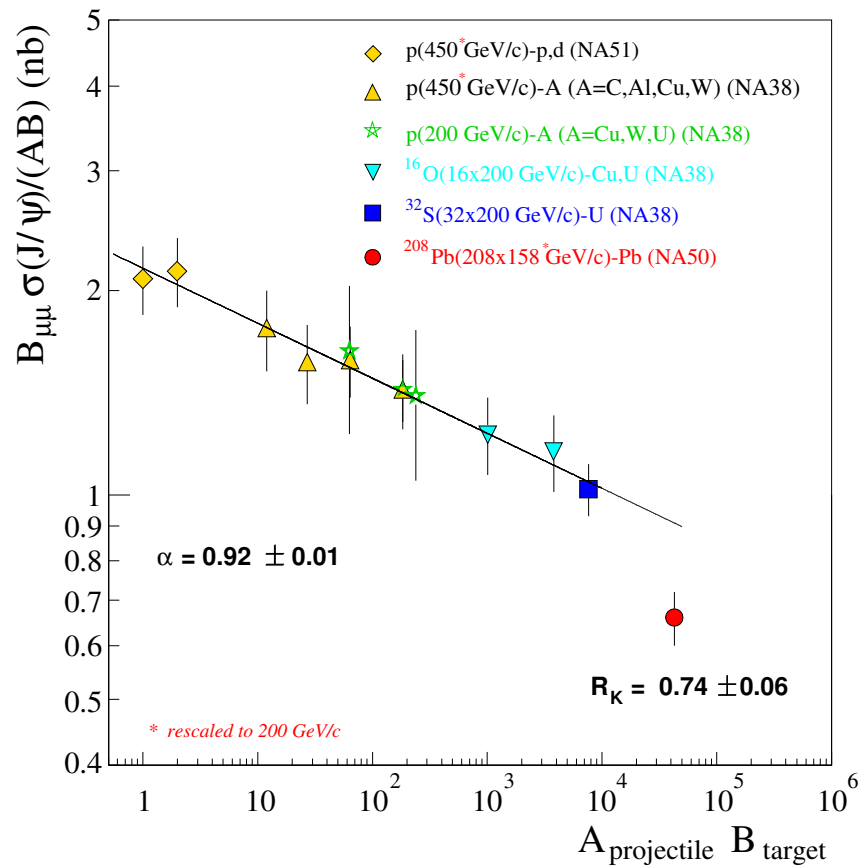


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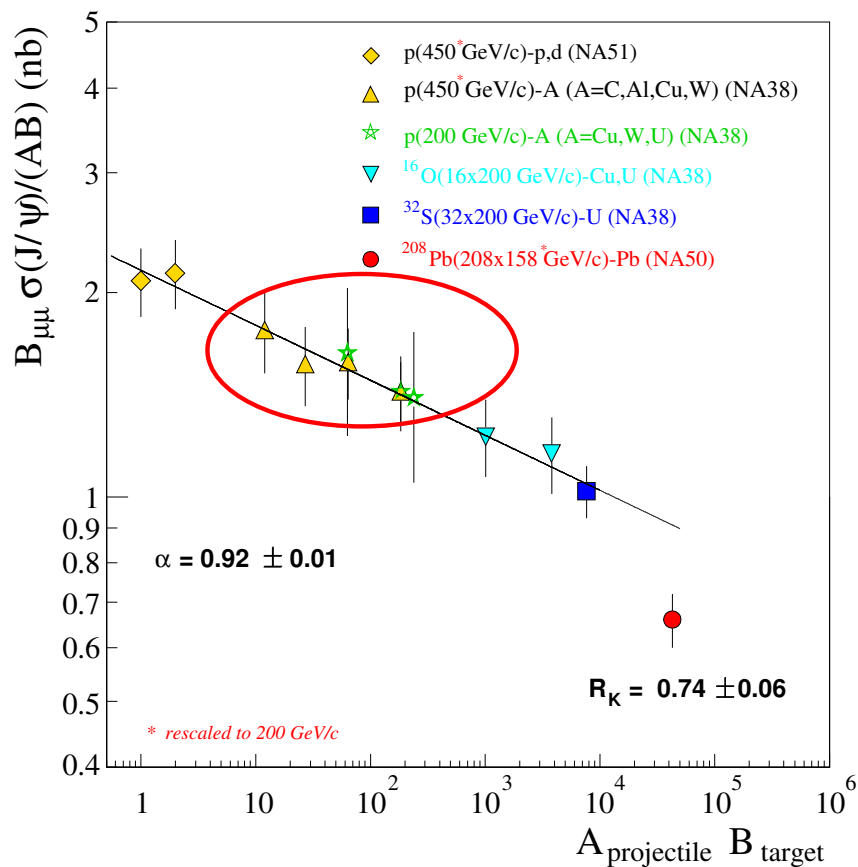


J/Ψ suppression II



⇒ J/Ψ suppression measured at CERN (NA50).

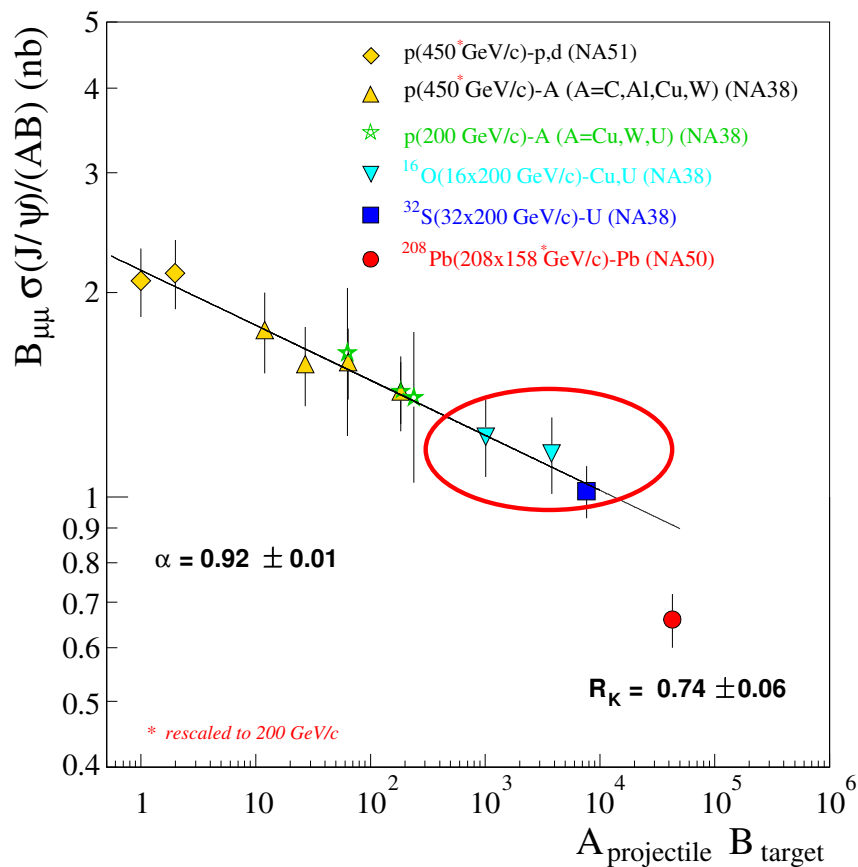
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$\Rightarrow J/\Psi$ suppression measured at CERN (NA50).

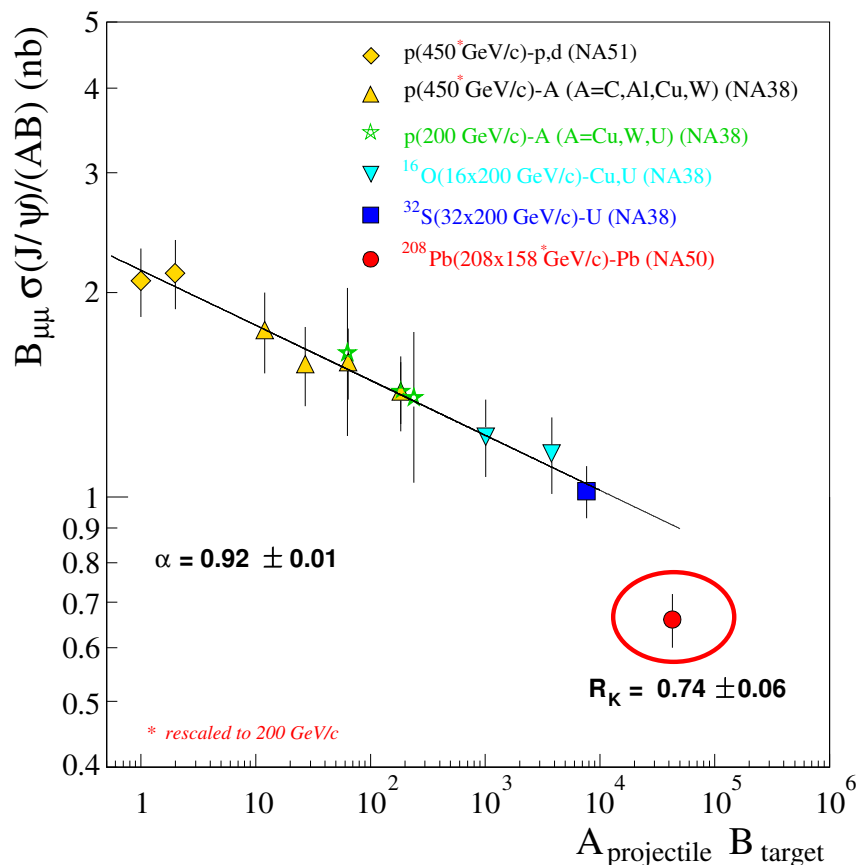
\Rightarrow pA collisions \rightarrow nuclear absorption. (multiple scattering $c\bar{c}$ -A)

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J/Ψ suppression II



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- ⇒ pA collisions → nuclear absorption. (multiple scattering $c\bar{c}$ -A)
- ⇒ OCu, OU, SU → nuclear absorption.
- ⇒ PbPb "anomalous suppression"
 ↘ hadronic or partonic origin?

Lattice results not yet determinant on whether J/Ψ dissociates at T_c or above. Other $c\bar{c}$ states, as ψ' or χ_c , could dissociate below T_c .

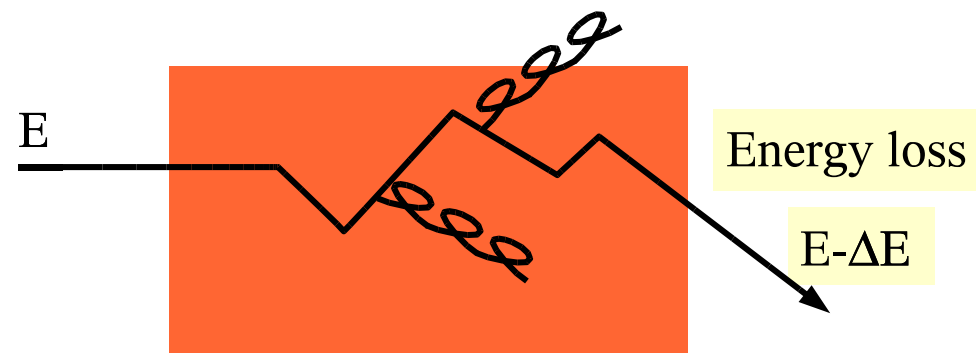
Jet quenching

Jet quenching

- ⇒ Suppose a particle entering a medium or created inside the medium

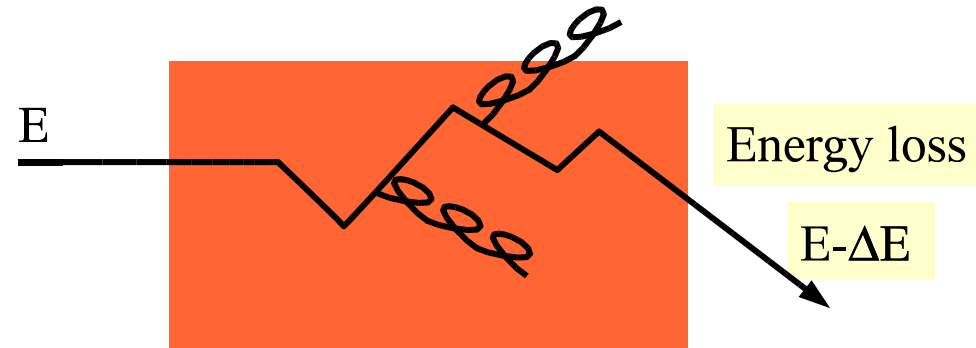
Jet quenching

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- ⇒ The particle loses energy while traveling through the medium
 - ↘ by scattering with the medium
 - ↘ by radiation



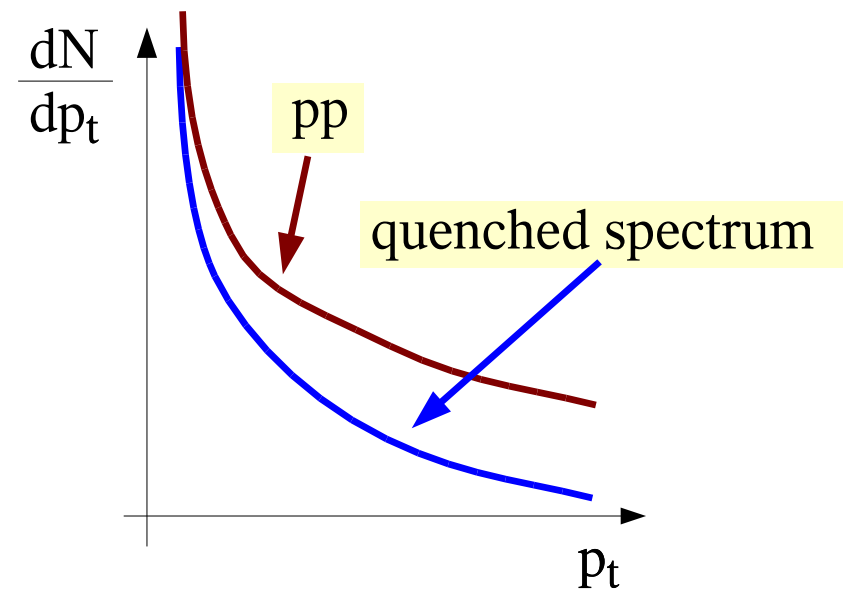
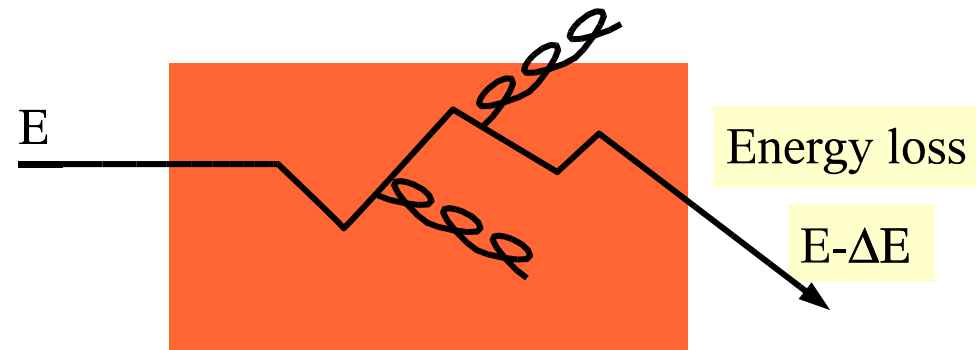
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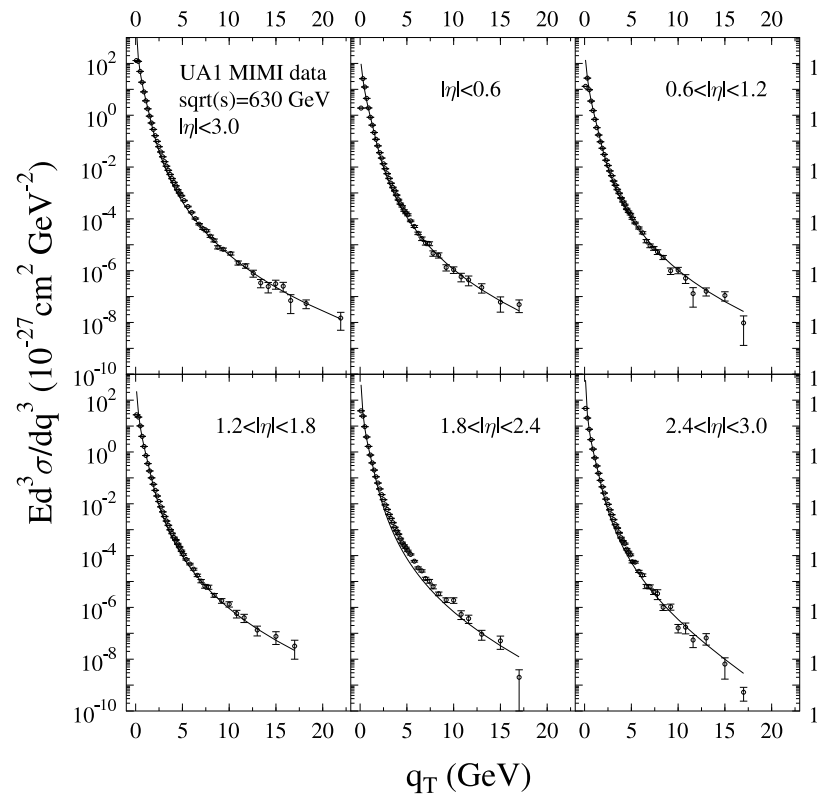
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- ⇒ A high- p_t particle produced inside a medium will lose energy while escaping it → spectrum suppressed at large p_t .



High- p_t production in pp: pQCD

QCD factorization formula:

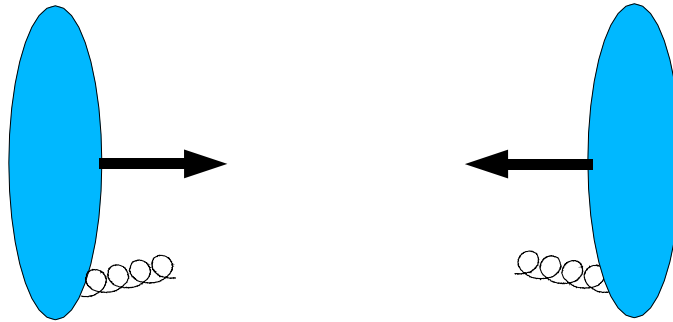
$$\frac{d\sigma_{pp}^h}{dp_t^2 dy} \sim \sum_{i,j} x_1 f_i^p(x_1, Q^2) \otimes x_2 f_j^p(x_2, Q^2) \otimes \frac{d\sigma^{ij \rightarrow k}}{d\hat{t}} \otimes D_{k \rightarrow h}(z, \mu_F^2)$$



(Eskola and Honkanen: Nucl.Phys. **A713** (2003) 167)

Space-time picture

Before the collision, initial state: nuclear PDF's.

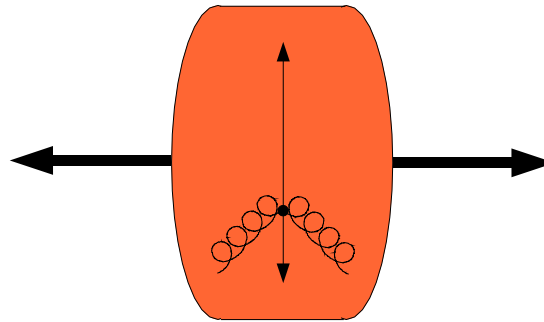


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Space-time picture

At $t \sim 0$

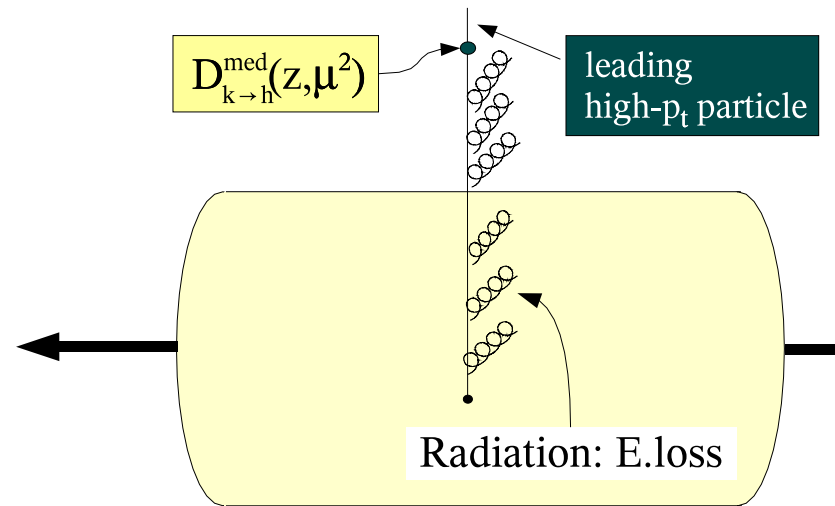


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Space-time picture

Evolution.

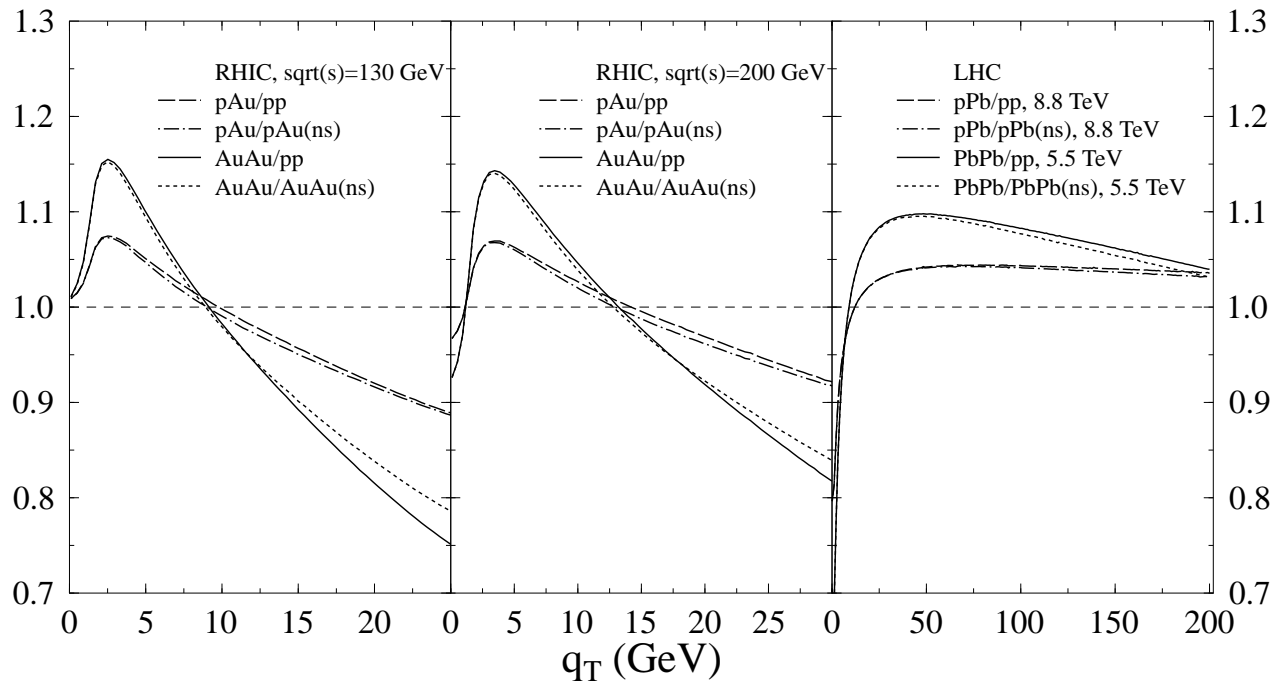


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Effects of nuclear PDF.

Nuclear effects in PDF produce small changes in high- p_t particle production at RHIC and LHC, **at most 25 %**.

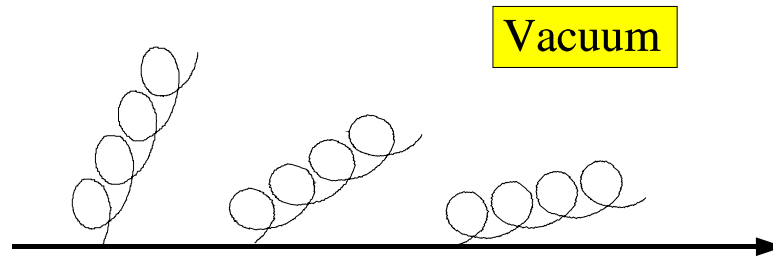


Computed using EKS98 nPDF's.

[Eskola and Honkanen]

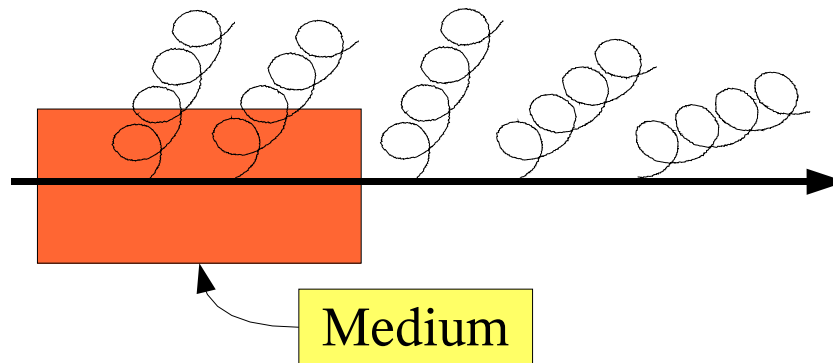
Matter affects evolution.

- ⇒ A quark or gluon (traveling in vacuum) with virtuality Q^2 will radiate gluons to become on-shell: DGLAP-like evolution.



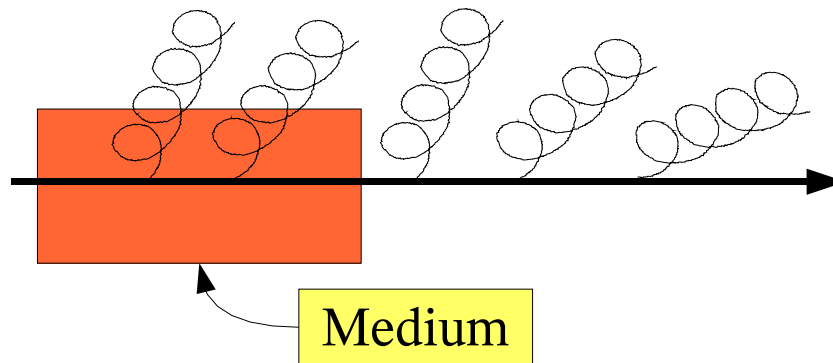
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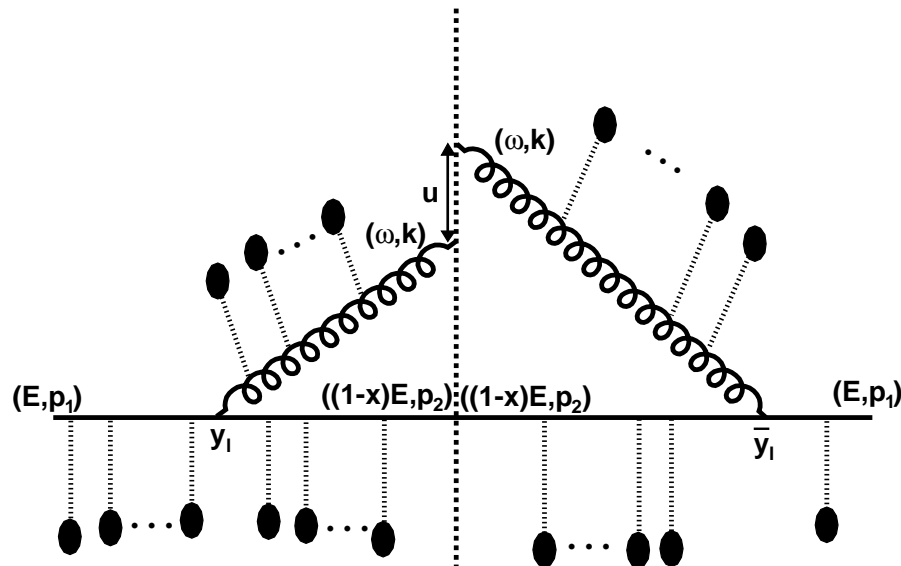
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- ⇒ Where to look?
 - ↘ Inclusive particle (suppression).
 - ↘ Jets: Jetshapes... → LHC

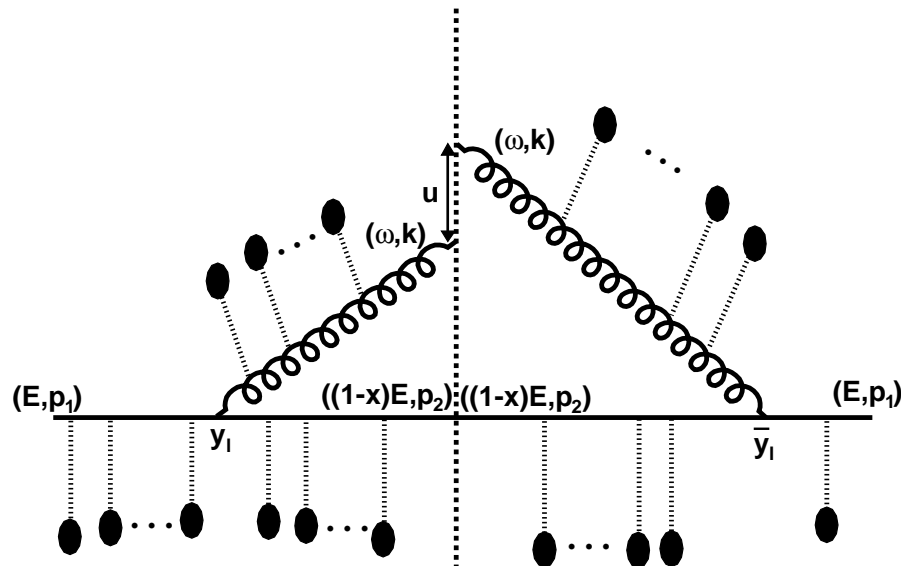
Medium-induced gluon radiation.



For media of finite length

$$\omega \frac{dI^{tot}}{d\omega dk_{\perp}^2} = \left| \begin{array}{c} \text{diagram} \\ 0 \quad L \end{array} \right|^2 + 2\text{Re} \left(\begin{array}{c} \text{diagram} \\ 0 \quad L \end{array} \right) \left(\begin{array}{c} \text{diagram} \\ \text{diagram} \end{array} \right)^* + \left| \begin{array}{c} \text{diagram} \\ \text{diagram} \end{array} \right|^2$$

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The medium induced gluon radiation

$$\omega \frac{dI}{d\omega dk_{\perp}^2} = \omega \frac{dI^{tot}}{d\omega dk_{\perp}^2} - \omega \frac{dI^{vac}}{d\omega dk_{\perp}^2}$$

Medium: L (length) and \hat{q} (transport coefficient).

Double differential spectrum

High energy approximation \longrightarrow multiple scattering. The final result is

$$\omega \frac{dI}{d\omega d\mathbf{k}_\perp} = \frac{\alpha_s C_R}{(2\pi)^2 \omega^2} 2\text{Re} \int_{\xi_0}^{\infty} dy_l \int_{y_l}^{\infty} d\bar{y}_l \int d\mathbf{u} e^{-i\mathbf{k}_\perp \cdot \mathbf{u}} e^{-\frac{1}{2} \int_{\bar{y}_l}^{\infty} d\xi n(\xi) \sigma(\mathbf{u})}$$
$$\times \frac{\partial}{\partial \mathbf{y}} \cdot \frac{\partial}{\partial \mathbf{u}} \int_{\mathbf{y}=0=\mathbf{r}(y_l)}^{\mathbf{u}=\mathbf{r}(\bar{y}_l)} \mathcal{D}\mathbf{r} \exp \left[i \int_{y_l}^{\bar{y}_l} d\xi \frac{\omega}{2} \left(\dot{\mathbf{r}}^2 - \frac{n(\xi) \sigma(\mathbf{r})}{i\omega} \right) \right].$$

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Two approximations

\Rightarrow Multiple soft scattering $n(\xi) \sigma(\mathbf{r}) = \frac{\hat{q}(\xi)}{2} \mathbf{r}^2$. The path integral reduces to a harmonic oscillator of imaginary frequency.

Double differential spectrum

High energy approximation \longrightarrow multiple scattering. The final result is

$$\omega \frac{dI}{d\omega d\mathbf{k}_\perp} = \frac{\alpha_s C_R}{(2\pi)^2 \omega^2} 2\text{Re} \int_{\xi_0}^{\infty} dy_l \int_{y_l}^{\infty} d\bar{y}_l \int d\mathbf{u} e^{-i\mathbf{k}_\perp \cdot \mathbf{u}} e^{-\frac{1}{2} \int_{\bar{y}_l}^{\infty} d\xi n(\xi) \sigma(\mathbf{u})}$$

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Two approximations

- \Rightarrow Multiple soft scattering $n(\xi) \sigma(\mathbf{r}) = \frac{\hat{q}(\xi)}{2} \mathbf{r}^2$. The path integral reduces to a harmonic oscillator of imaginary frequency.
- \Rightarrow Single hard scattering First order in the **opacity expansion parameter** $n(\xi) \sigma(\mathbf{r})$. A Yukawa cross section is usually taken for the cross section $\sigma(\mathbf{r})$
- \Rightarrow Expansion in the number of scatterings

Coherent radiation

Two phases appear: quark and emitted gluon

$$\varphi_E = \left\langle \frac{k_{\perp}^2}{2E} \Delta z \right\rangle \quad \varphi = \left\langle \frac{k_{\perp}^2}{2\omega} \Delta z \right\rangle \implies l_{coh} \sim \frac{\omega}{k_{\perp}^2}$$

High energy limit $E \rightarrow \infty$ so, the first one is neglected.

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Let us define $\kappa^2 \equiv \frac{k_{\perp}^2}{\hat{q}L}$, $\omega_c = \frac{1}{2} \hat{q} L^2$

So, the phase for $\Delta z = L \rightarrow \varphi \sim \kappa^2 \frac{\omega_c}{\omega}$

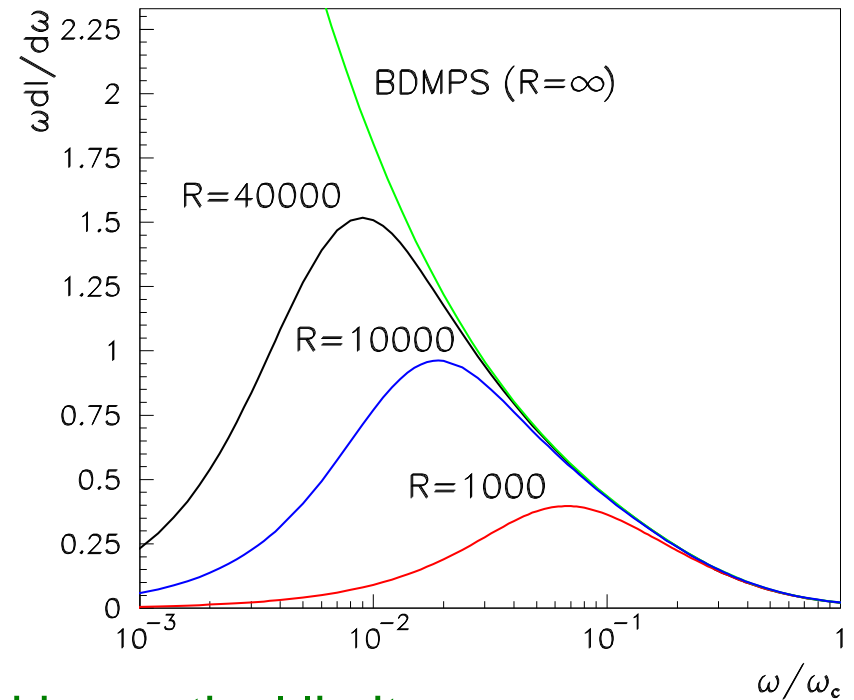
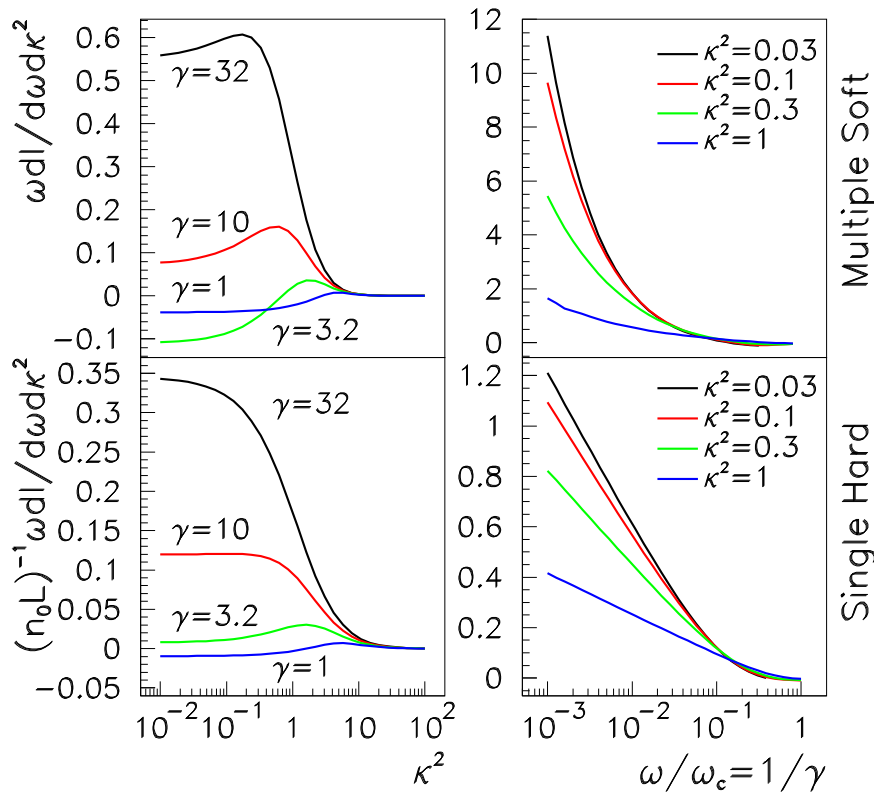
gluon emitted when $\varphi \gtrsim 1 \iff$ radiation suppressed for $\kappa^2 \lesssim \omega/\omega_c$

In cold nuclear matter: $Q_{sat}^2 = \hat{q}L \implies \kappa^2 = \frac{k_{\perp}^2}{Q_{sat}^2}$

Gluon energy distributions for quark jets

$$\kappa^2 = \frac{k_{\perp}^2}{\hat{q}L}, \quad \omega_c = \frac{1}{2}\hat{q}L^2$$

$$\omega \frac{dI}{d\omega} = \int_0^{\omega} dk_{\perp} \omega \frac{dI}{d\omega dk_{\perp}}$$



Plateau at small $\kappa \longleftrightarrow$ coherence
 gluons \implies factor N_c/C_F larger

kinematical limit

$k_{\perp} \leq \omega \implies R = \omega_c L$ finite

Infrared safe.

Properties of the spectrum

- ⇒ For gluon emission, we have the restriction $k_{\perp} \leq \omega$.
- ⇒ Coherence, $k_{\perp}^2 \lesssim \hat{q}L$. \implies spectrum suppressed for

$$\omega^2 \lesssim k_{\perp}^2 \sim \hat{q}L \quad \iff \quad \left(\frac{\omega}{\omega_c}\right)^2 \lesssim \frac{2}{R}, \quad R = \frac{1}{2}\hat{q}L^3.$$

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→ Formation time effects suppress IR region.

⇒ Removing this limit ($R \rightarrow \infty$)

$$\lim_{R \rightarrow \infty} \omega \frac{dI(\omega)}{d\omega} = \frac{\alpha_s C_R}{\pi} \ln \left[\cosh^2 \sqrt{\frac{\omega_c}{2\omega}} - \sin^2 \sqrt{\frac{\omega_c}{2\omega}} \right].$$

[Baier, Dokshitzer, Mueller, Peigné, Schiff]

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[Baier, Dokshitzer, Mueller, Peigné, Schiff]

⇒ The total energy loss:

$$\lim_{R \rightarrow \infty} \omega \frac{dI(\omega)}{d\omega} \xrightarrow{\omega < \omega_c} \sqrt{\frac{\omega_c}{\omega}} \quad \iff \quad \Delta E = \int d\omega \omega \frac{dI(\omega)}{d\omega} \sim \omega_c \sim \hat{q}L^2$$

Medium-modified fragmentation functions I

⇒ For large- p_t the hadronization takes place outside the medium

⇒ Model: (Wang, Huang, Sarcevic, PRL 77 2537)

$$D_{h/q}^{(\text{med})}(z, Q^2) = \int_0^1 d\epsilon P_E(\epsilon) \frac{1}{1-\epsilon} D_{h/q}\left(\frac{z}{1-\epsilon}, Q^2\right).$$

⇒ $P(\epsilon)$ probability that the hard parton loses a fraction of energy ϵ .

⇒ Independent gluon emission approx.: (BDMS, JHEP 0109:033)

$$P_E(\epsilon) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[\prod_{i=1}^n \int d\omega_i \frac{dI(\omega_i)}{d\omega} \right] \delta\left(\epsilon - \sum_{i=1}^n \frac{\omega_i}{E}\right) \exp\left[-\int d\omega \frac{dI}{d\omega}\right].$$

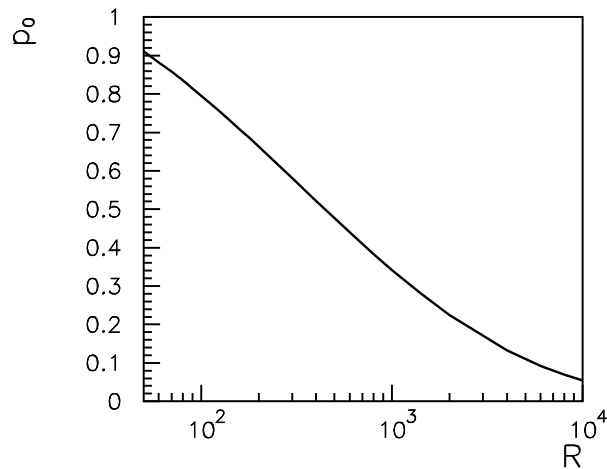
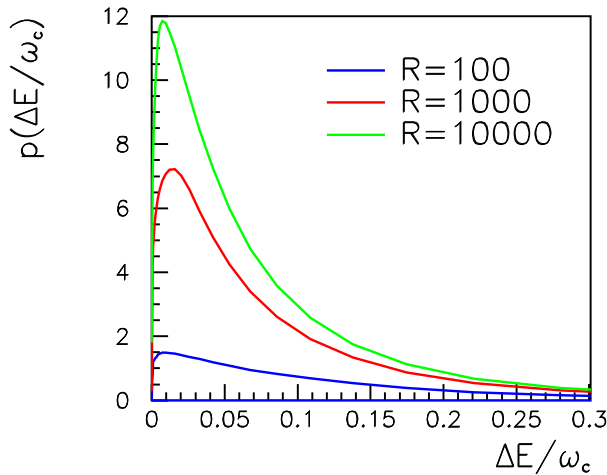
$$P(\epsilon) = p_0 \delta(\epsilon) + p(\epsilon)$$

↘ $p_0 \Rightarrow$ no E.loss

↘ $p(\epsilon) \Rightarrow$ sum for $n \geq 1$.

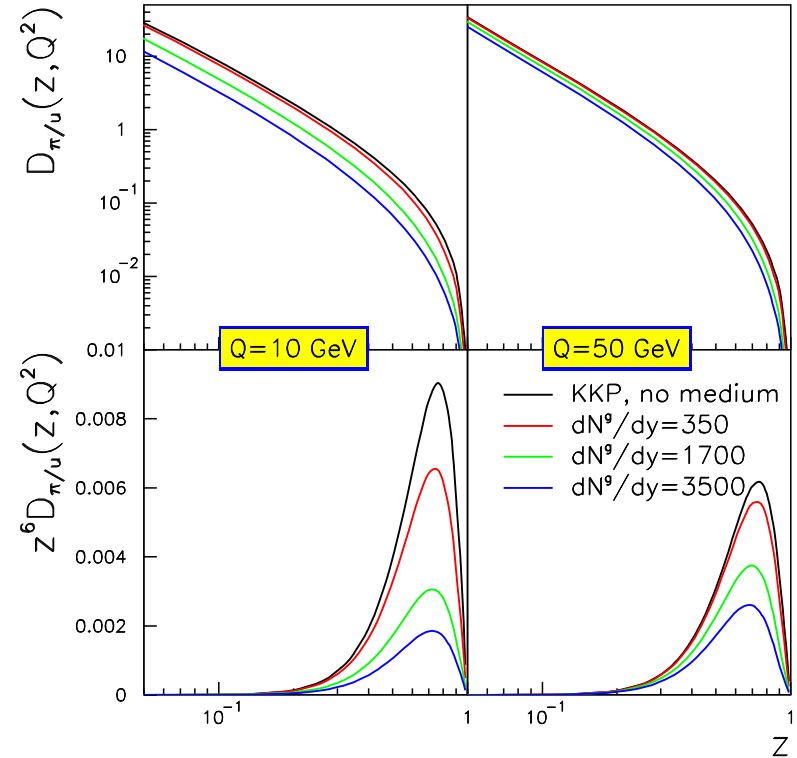
Medium-modified FF II

Quenching weights for quarks.



Tabulated: <http://home.cern.ch/csalgado>

$$R = \frac{\bar{q}}{2} L^3 = \frac{L^2}{R_A^2} \frac{dN^g}{dy}$$



Suppression of ~ 5 for $p_t \sim 5 \div 7$ GeV $\implies R \sim 2000$.

Comparison with PHENIX data.

⇒ At RHIC, particles with $p_t \lesssim 10$ GeV have been measured.

⇒ Ratio with proton-proton:

$$R_{AA} = \frac{dN^{AA}/dp_t}{N_{\text{coll}}dN^{pp}/dp_t}$$

$R_{AA} = 1 \Rightarrow$ no effect.

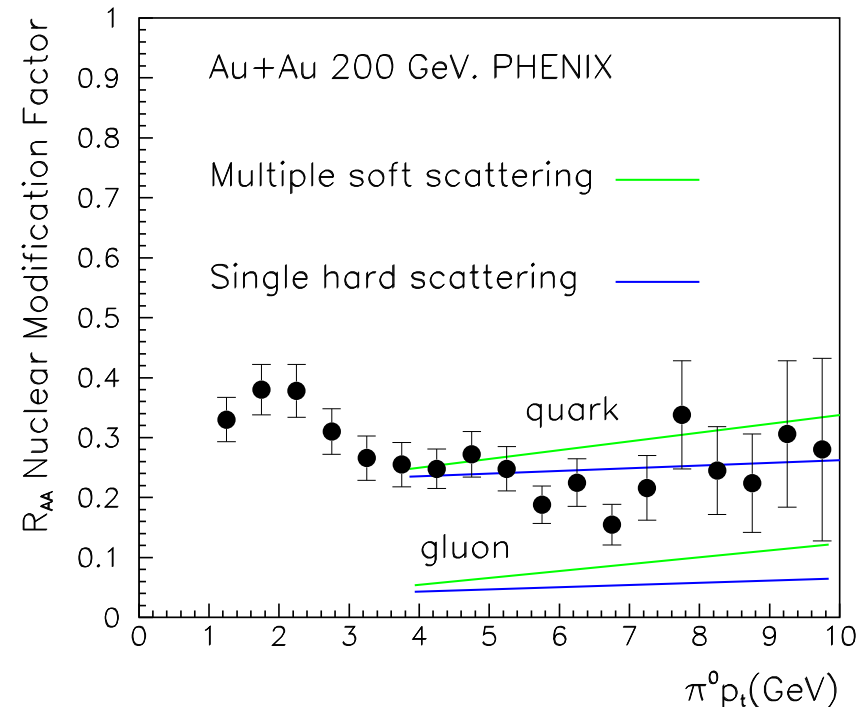
⇒ A factor of 5 suppression for central AuAu collisions.

⇒ Smallest values of p_t are in the limit of applicability of the calculations.

⇒ Can be described with $dN^g/dy \sim 1000 \div 2000$.

⇒ Some estimates [X-N Wang]

$$\epsilon|_{\tau \sim 0.2 fm/c} \sim 15 GeV/fm^3$$



Summary III

- ⇒ In order to characterize the created medium (indirect) signals are necessary.
 - ↪ Soft: strangeness enhancement, particle ratios, flows
 - ↪ Hard: J/Ψ suppression, jet quenching
- ⇒ Hard probes specially interesting as
 - ↪ they are created at very short times $\sim 1/Q$
 - ↪ can be described by perturbative QCD
- ⇒ All these effects have been measured in nucleus-nucleus collisions, however, they can also be produced by
 - ↪ Nuclear effects in the initial state (shadowing...)
 - ↪ Interaction with a **confined** medium (pion gas...)
- ⇒ Study proton-nucleus collisions as a control experiment.